# Round Table on Coherence (Part I)

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<sup>1</sup>These slides include joint work with Daniel Berntson (Princeton), Rachael Briggs (ANU), Fabrizio Cariani (NU), Kenny Easwaran (USC), and David McCarthy (HKU). Please do not cite or quote without permission.

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• Today's Round Table is about a new way of thinking about formal, epistemic coherence requirements, which was inspired by Jim Joyce's [10, 9] arguments for *probabilism*.

• Richard will tell us about such arguments for probabilism.

- I'm going to explain how to generalize Joyce's idea to *any* type of judgment that can be assessed in terms of *accuracy*.
- Then, I will describe how this framework applies to *full belief* (this is joint work with Kenny Easwaran [1, 2]).
- The framework has also been applied to comparative confidence (that is joint work with David McCarthy [7]).
  - All three of these applications of the general framework are described in detail in the notes from my recent seminar here at MCMP. See: http://fitelson.org/coherence.
- Let's begin by thinking about coherence requirements for full belief. The traditional/classical story is that *deductive consistency* is a/the coherence requirement for full belief.

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- Notation: *B*(*p*) [*S* believes that *p*], *D*(*p*) [*S* disbelieves that *p*], and **B** [the set of *all* of *S*'s beliefs and disbeliefs]. For simplicity, we assume that *S* is *finite and opinionated*.
- Here, I will use the word "reasonable" to mean "supported by one's evidence" (for now, in an informal, intuitive sense).
- Unfortunately, deductive consistency is implicated in some infamous *paradoxes e.g.*, the Lottery and the Preface.
  - Lottery Paradox ([12],[6]). For each ticket *i*, it is highly probable that *i* is a loser (*L<sub>i</sub>*). So, it would seem reasonable to be such that *B*(*L<sub>i</sub>*), for each *i*. However, this inevitably renders our set *3 inconsistent*, since we *know* that (∃*i*)(¬*L<sub>i</sub>*).
  - Preface Paradox ([14],[4]). Let B ⊂ B be the set containing *all* of your *reasonable* (1<sup>st</sup>-order) beliefs. This B is an incredibly rich and complex set of judgments. You're fallible (*i.e.*, your 1<sup>st</sup>-order evidence is *sometimes misleading*). So, it seems reasonable to believe that *some B*'s in B are false. However, adding *this* (2<sup>nd</sup>-order) belief to B renders B *inconsistent*.

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- Typically, such "paradoxes" involve a *conflict* between a *consistency* requirement and an *evidential* requirement, which requires *believing what is evidentially supported*.
- There are various responses to such paradoxes.
- Some ([15], [13]) try to *maintain* consistency as a CR.
  - Such approaches tend to have implausible consequences about the nature of evidential support/reasonable belief.
- Some ([11], [4]) say there are no CRs (per se) for full belief.
  - These approaches have more plausible things to say about evidential support/reasonable belief, but they *give up* on trying to articulate coherence requirements for full belief.
- I (we) would suggest that such paradoxes indicate that the classical CR for full belief is *too strong*. What we need is an *alternative story* about coherence requirements.
  - Ideally, we want coherence requirements for full belief that are entailed by both alethic and evidential considerations.

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- For each proposition *p* in some finite Boolean algebra *B*, *S* will be such that *either B*(*p*) or *D*(*p*) *and not both*.
- To make things *really* simple, we'll assume  $D(p) \equiv B(\neg p)$ .
- Finally, we'll use **3** to denote the *entire* set of judgments (beliefs and disbeliefs) made by *S* over the *full* algebra *B*.
- With this background in place, applying our new framework to full belief involves going through the following *3 steps*.
- Step 1: Define the vindicated (viz., perfectly accurate) judgment set, at w. ["Judgments of the omniscient S at w."]

•  $\mathring{\mathcal{B}}_w$  contains B(p) [D(p)] iff p is true (false) at w.

- Step 2: Define a notion of "distance between B and B<sub>w</sub>". That is, a measure of *distance from vindication* d(B,B<sub>w</sub>).
  - $d(\mathfrak{B}, \mathfrak{B}_w) \cong$  the number of inaccurate judgments in  $\mathfrak{B}$  at w.
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  - To make things *really* simple, we'll assume  $D(p) \equiv B(\neg p)$ .
  - Finally, we'll use  $\mathfrak{B}$  to denote the *entire* set of judgments (beliefs and disbeliefs) made by *S* over the *full* algebra  $\mathcal{B}$ .
- With this background in place, applying our new framework to full belief involves going through the following *3 steps*.
- **Step 1**: Define the *vindicated* (*viz., perfectly accurate*) *judgment set*, at *w*. ["Judgments of the omniscient *S* at *w*."]

• **Step 2**: Define a notion of "distance between  $\mathfrak{B}$  and  $\mathfrak{B}_w$ ". That is, a measure of *distance from vindication*  $d(\mathfrak{B}, \mathfrak{B}_w)$ .

•  $d(\mathfrak{B}, \mathfrak{B}_w) \cong$  the number of inaccurate judgments in  $\mathfrak{B}$  at w.

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Stage-Setting	The Framework	New Coherence Requirements for 33
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**Possible Vindication** (PV). There exists *some* possible world w at which *all* of the judgments in  $\mathfrak{B}$  are accurate. Or, to put this more formally in terms of d:  $(\exists w)[d(\mathfrak{B}, \mathring{\mathfrak{B}}_w) = 0]$ .

- Possible vindication is *one way* we could go here. But, our framework is *much more general* than the classical one. It allows for *many other* choices of fundamental principle.
- Inspired by the work of de Finetti [5] and Joyce [10], we can *back away* from (PV) to something weaker, but still probative *the avoidance of (weak) dominance in d*(B, B<sub>w</sub>).

Weak Accuracy-Dominance Avoidance (WADA).

There does *not* exist an alternative belief set  $\mathfrak{B}'$  such that: (i)  $(\forall w) [d(\mathfrak{B}', \mathring{\mathfrak{B}}_w) \le d(\mathfrak{B}, \mathring{\mathfrak{B}}_w)]$ , and

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Completing Step 3 in this way leads to a new CR for 3.

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• Completing Step 3 in *this* way leads to a *new* CR for **B**.

- The new coherence requirement implied by this application of our framework has just the sort of properties we wanted.
- We wanted a coherence requirement that (like consistency) was motivated by considerations of accuracy (ideally, *entailed by* alethic requirements such as consistency/PV).
- But, we also wanted a coherence requirement that was *strictly weaker* than deductive consistency in such a way that it is *also entailed by our evidential requirements*.
- Happily, it can be shown that we have met both of these *desiderata*, provided that we accept the following weak assumption about our evidential requirements.
  - Evidential Requirement for Belief (EB). An agent S (with total evidence E<sub>S</sub>) meets her evidential requirements only if there exists some Pr-function [Pr(+|E<sub>S</sub>)] which probabilifies each of her beliefs and dis-probabilifies each of her disbeliefs.
- There is disagreement about which Pr(· | E<sub>S</sub>) should do the (dis)probabilifying [3, 16, 8], but there is agreement on (EB)

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-Setting		The Framework 00	New Coherence Requiremen ○●	its for 33
۲	• Here are the logical relationships between key norms:			
		The Truth Norm fo	or Belief:	(TB) ↓ ∦

tting	The Framework 00	New Coherence Requiremen ○●	nts for <b>B</b>
• He	• Here are the logical relationships between key norms:		
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ting		The Framework 00	New Coherence Requiremer ○●	nts for 23
•	• Here are the logical relationships between key no			norms:
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ing		The Framework oo	New Coherence Requiremer ○●	nts for 33
•	Here	e are the logical relatio	nships between key	norms:
		The Truth Norm for 1	3elief:	(TB) ↓ ∳
		Possible Vindication	( <i>viz.</i> , consistency):	(PV) ↓ ∦

age-Setting 00	The Framework 00	New Coherence Requireme ○●	nts for 33
• He	ere are the logical relat	ionships between key	norms:
	The Truth Norm fo	r Belief:	(TB)
	Possible Vindicatio	n ( <i>viz.</i> , consistency):	↓ ∱ (PV) ↓ ∱

age-Setting 00		The Framework 00	New Coherence Requiremen ○●	its for 33
۲	Here	are the logical relations	hips between key	norms:
		The Truth Norm for Bel	ief:	(TB)
		Possible Vindication (vi	z., consistency):	↓ ∲ (PV) ↓ ∳

age-Setting 00	The Framework 00	New C ○●	Coherence Requirement	nts for B
• Here	are the logical rela	ationships	between key	norms:
	The Truth Norm f	or Belief:		(TB)
	Possible Vindicati	on ( <i>viz.</i> , co	onsistency):	↓ γ <sup>†</sup>
R?	Weak Accuracy-De	ominance A	Avoidance:	(WADA)

tage-Setting	The Framework oo	New Coherence Requiremen ○●	ts for B
9	• Here are the logical relationships between key norms:		
	The Truth Norm fo	or Belief:	(TB)
	Possible Vindicatio	on ( <i>viz.</i> , consistency):	↓ ↑ (PV)
	🕼 Weak Accuracy-Do	minance Avoidance:	₩ ∯ (WADA)
			1 ↓

tage-Setting 00	The Framework New Coherence ○○ ○●	e Requirements for 3
• He	re are the logical relationships betw	een key norms:
	The Truth Norm for Belief:	(TB)
	Possible Vindication ( <i>viz.</i> , consist	↓ ∦ ency): (PV) ↓ ∦
R <sup>3</sup>	Weak Accuracy-Dominance Avoid	lance: (WADA)
		↑ ¥ (EB)

tage-Setting 900	The Framework 00	New Coherence Requiremen ○●	nts for B
• Her	e are the logical relati	onships between key	norms:
	The Truth Norm for	Belief:	(TB)
	Possible Vindication	ı ( <i>viz.</i> , consistency):	ψη (PV) ψη∕
ß	Weak Accuracy-Don	ninance Avoidance:	(WADA)
	Evidential Requirem	ent for Belief:	↑ ¥ (EB)

age-Setting 00	The Framework 00	New Coherence Requiremen ○●	nts for B
• He	ere are the logical relat	ionships between key	norms:
	The Truth Norm fo	r Belief:	(TB)
	Possible Vindicatio	n ( <i>viz.</i> , consistency):	(PV) ↓ 1∕r
ß	> Weak Accuracy-Do	minance Avoidance:	(WADA)
	Evidential Requirer	nent for Belief:	1r ∳ (EB)

age-Setting oo	The Framework 00	New Coherence Requiremer ○●	nts for B
• He	re are the logical rela	tionships between key	norms:
	The Truth Norm fo	r Belief:	(TB) ↓ ∦
	Possible Vindicatio	n ( <i>viz.</i> , consistency):	(PV) ↓ ∦
ß	Weak Accuracy-Do	minance Avoidance:	(WADA)
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ge-Setting o	The Framework 00	New Coherence Requiremer ○●	nts for B
• Her	e are the logical rela	tionships between key	norms:
	The Truth Norm fo	or Belief:	(TB) ↓ 1∕r
	Possible Vindicatio	on ( <i>viz.</i> , consistency):	(PV) ↓ ∦
ß	Weak Accuracy-Do	minance Avoidance:	(WADA)
	Evidential Require	ment for Belief:	1⊧ ∳ (EB)



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Stage-Setting	The Framework	New Coherence Requirements for <b>B</b>		Rei
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